

2021

B.C.A

[HONOURS]

Paper : BCA-301

(Mathematics)

Full Marks : 80

Time : 4 Hours

*The figures in the right-hand margin indicate marks.**Candidates are required to give their answers in their own words as far as practicable.*Answer **Q. No. 1** and any **four** from the rest.1. Answer any **eight** questions:  $2 \times 8 = 16$ 

- a) Find the mode of 2, 1, 3, 2, 5, 3, 2, 4, 2, 1, 6.
- b) Define Absolute error and Relative Percentage error.
- c) Write down the p.d.f. of Binomial distribution.
- d) State Baye's theorem.
- e) Find the mean of the distribution given by the

$$\text{p.d.f. } f(x) = \begin{cases} x^2, & 0 \leq x < 1 \\ 0, & \text{elsewhere} \end{cases}$$

f) Round-off the following numbers to four significant figures:

i) 3.92542

ii) 40.358

iii) 0.98735

iv) 0.0058425

g) Define degree of Precision in numerical integration.

h) What is extrapolation?

i) Write down the p.d.f. of Normal distribution.

j) If  $x = 3y - 6$  and  $2y = 3x - 8$  are regression equation of  $x$  on  $y$  and  $y$  on  $x$  respectively. Find the correlation coefficient between  $x$  and  $y$ .

k) What are the advantages of Lagrange interpolation formula over Newton's forward interpolation formula?

l) Define conditional probability.

2. a) Define Poisson distribution and find its mean and variance.

b) Person A speaks truth 60% cases, and person B speaks truth in 80% cases, what is the

percentage of cases they likely to contradict each other while narrating some incident?

c) Prove that for any two events A and B  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ .

$$8+5+3=16$$

3. a) Calculate the mean, median and mode of the following frequency distribution:

<b>Height (inch)</b>	56-60	61-65	66-70	71-75
<b>No. of Persons</b>	15	40	30	5

b) The second order moment of a random variable X is minimum when taken about mean.

$$10+6=16$$

4. a) Calculate the arithmetic mean and standard deviation of the following frequency distribution:

<b>Class interval:</b>	0-9	10-19	20-29	30-39	40-49	50-59
<b>Frequency:</b>	15	20	25	24	12	34

b) Calculate the median and mode of the following frequency distribution:

<b>Height(inch):</b>	60-64	65-69	70-74	75-79	80-84	85-89
<b>No. of Persons:</b>	8	28	118	66	16	8

$$8+8$$

5. Write an algorithm to find the solution of system of 3 linear equations in 3 unknowns by Gauss-Seidel iteration method. Use this method to solve the

$$4x_1 - x_2 - x_3 = -7$$

$$x_1 - 5x_2 + x_3 = -10$$

$$x_1 + 2x_2 + 6x_3 = 9 \quad 8+8$$

6. Develop an algorithm to evaluate the integral

$$\int_a^b f(x) dx \text{ by trapezoidal rule and hence evaluate}$$

$$\int_{-1}^1 \frac{dx}{1+x^2} \text{ taking 8 sub-interval.} \quad 10+6$$

7. a) Develop an algorithm to solve initial value problem by 2nd order R-K method.

b) Use 2nd order R-K method to calculate Y(0.2) from the initial value problem

$$\frac{dy}{dx} = x + y^2, y(0)=1 \text{ (taking } h=1). \quad 8+8$$