

**Raghunathpur College**

**Internal Examination-2020**

**Mode of Examination: Assignment writing**

**Subject: Mathematics**

**Paper: BMTMCCHT301 (Real analysis-II)**

**Full Marks: 10**

**Answer any one questions:  $10 \times 1 = 10$**

1. (a) Define uniform continuity of a function of real variable.

(b) If  $f : [0,1] \rightarrow \mathbb{R}$  is continuous and assumes rational values only and  $f(\frac{1}{3}) = \frac{1}{3}$ , then show that  $f(x) = \frac{1}{3}$  for all  $x \in [0,1]$ .

(c) Examine whether the function  $f(x, y) = \begin{cases} 2xy \frac{x^2 - y^2}{x^2 + y^2} & \text{if } (x, y) \neq (0, 0) \\ 0 & \text{if } (x, y) = (0, 0) \end{cases}$

Is continuous at  $(0, 0)$ .

2+3+5=10

2(a). Define maxima of a function in an interval.

(b) Show that the minimum value of  $\frac{(2x-1)(x-8)}{x^2-5x+4}$  is greater than its maximum value.

(c) A function  $f$  is defined on  $\mathbb{R}$  by  $f(x) = x^2 \sin \frac{1}{x}$ ,  $x \neq 0$  and  $f(0) = 0$ . Show that  $f$  is differentiable on  $\mathbb{R}$  but  $f'$  is not continuous on  $\mathbb{R}$ .

2+4+4=10